

## Solutions: The Graph of a Rational Function variation

$$\begin{aligned}
 1.) \quad A.) \quad C &= (\text{cost of top \& bottom}) + (\text{Cost of side}) \\
 &= (2\pi r^2 \text{ cm}^2) \left( \frac{0.05 \text{ ¢}}{\text{cm}^2} \right) + (2\pi r h \text{ cm}^2) \left( \frac{0.02 \text{ ¢}}{\text{cm}^2} \right) \\
 &\quad \downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \\
 &\quad \text{Total area} \quad \text{Cost/unit} \quad \text{Total area} \quad \text{Cost/unit} \\
 &\quad \text{of top \& bottom} \quad \text{Area} \quad \text{of side of can} \quad \text{Area}
 \end{aligned}$$

$$= \underline{0.10\pi r^2 + 0.04\pi r h}$$

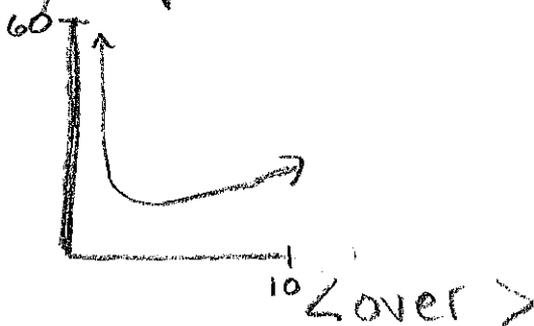
- Since we have to express cost in terms of  $r$ , we need to use the volume of a cylinder formula, sub in 500 and solve for  $h$ .
- Then sub the  $h$  equation in for  $h$  in the equation above, then simplify.

$$V = \pi r^2 h \rightarrow 500 = \pi r^2 h \rightarrow \left( \frac{500}{\pi r^2} = h \right)$$

$$C(r) = 0.10\pi r^2 + 0.04\pi r \left[ \frac{500}{\pi r^2} \right]$$

$$C(r) = 0.10\pi r^2 + \frac{20}{r} \quad \text{or} \quad \frac{0.10\pi r^3 + 20}{r}$$

B.) Graph  $C(r)$  of calculator



C.) use Min function on calc to get (3.17, 9.47)

$$r = 3.17 \text{ cm}$$

$$d.) \text{ least cost } \approx 9.47 \text{ ¢}$$

2.) A.) Because  $w$  varies inversely with  $L$ , we know that  $W = \frac{K}{L}$

• Sub in 500 for  $W$  + 10 for  $L$ , and solve for  $K$ . Then sub in for  $K$  in the equation above.

$$500 = \frac{K}{10} \rightarrow 10 \cdot 500 = \frac{K}{10} \cdot 10$$

$$\underline{5000 = K}$$

$$\rightarrow \boxed{W(L) = \frac{5000}{L}}$$

B.) To find the max weight, sub 25 in for  $L$  and solve for  $W$

$$W(25) = \frac{5000}{25} \rightarrow \boxed{W = 200 \text{ lbs}}$$

3.)  $L$  = heat loss,  $T$  = temp. difference,  $A$  = area of wall,  $d$  = thickness of wall

$$\boxed{L = K \cdot \frac{AT}{d}} \text{ where } K \text{ is the constant of proportionality}$$

4.)  $F = K \cdot Av^2 \rightarrow$  since  $F$  varies jointly w/  $A$  and  $v^2$

$$150 = K \cdot (4 \cdot 5)(30)^2 \rightarrow \boxed{K = \frac{1}{120}}$$

$$F = \frac{1}{120} Av^2 \rightarrow \text{Sub (3.4) in for } A \text{ and } 50 \text{ mph}$$

for  $v \rightarrow F = \frac{1}{120} (3 \cdot 4)(50)^2 = \boxed{250 \text{ lbs}}$